VU Rendering SS 2015 186.101

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VU Rendering SS 2015 Unit 05 – Participating Media







Light interaction with surfaces:

$$L_o(x,\vec{\omega}) = \underbrace{L_e(x,\vec{\omega})}_{emitted} + \underbrace{\int_{\Omega} L_i(x,\vec{\omega}') f_r(\vec{\omega}, x, \vec{\omega}') \cos \theta \ d\vec{\omega}'}_{emitted}$$

 $reflected \ incoming \ light$







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Assumes:

- Interaction directly at the surface (true for metals)
- No interaction with the volume in between (true for vacuum)









Water









Surface approxiation not always valid \rightarrow need to extend our model of light transport for materials that

allow perceivable light penetration andperceivably interact with light.







absorption

















- absorptionemission
- out-scattering







- absorption
- emission
- out-scattering
- in-scattering







- absorption
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$$(\vec{\omega} \cdot \nabla) L(x, \vec{\omega}) = ?$$

 $= -\sigma_a(x)L(x,\vec{\omega})$

 $= -\sigma_s(x)L(x,\vec{\omega})$

 $=\varepsilon(x)$

- absorption
- emission
- out-scattering









Phase Function

For incoming direction $\vec{\omega}'$ how much radiance is scattered into direction $\vec{\omega}$?

- Phase function: $p(x, \vec{\omega}, \vec{\omega}')$
- Depends on the material
 - Size of particles
 - Geometry of particles
- Normalized, i.e., $\int_{A_{-}} p(x, \vec{\omega}, \vec{\omega}') d\vec{\omega}' = 1$

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Phase Function



Henyey-Greenstein

- Interstellar dust
- Analytic
- Anisotropy g



Schlick Approxim. $p(\theta) = \frac{1}{4\pi} \frac{1 - k^2}{(1 - k\cos(\theta))^2}, k = 1.55g - 0.55g^3$

Lorenz-Mie Scattering

- Spherically homogeneous particles
- Full electrodynamic computation





Rayleigh Scattering

- Small particle approximation of Lorenz-Mie
- Covers scattering by pure air
- Depends on the light's wavelength



















Also known as Radiative Transport Equation

$$\begin{split} (\vec{\omega} \cdot \nabla) L(x, \vec{\omega}) &= -\underbrace{\sigma_a(x) L(x, \vec{\omega})}_{\text{absorption}} - \underbrace{\sigma_s(x) L(x, \vec{\omega})}_{\text{out-scattering}} + \underbrace{\varepsilon(x)}_{\text{emission}} \\ &+ \underbrace{\sigma_s(x) \int_{4\pi} p(x, \vec{\omega}, \vec{\omega}') L(x, \vec{\omega}') d\vec{\omega}'}_{\text{in-scattering}} \end{split}$$







Also known as Radiative Transport Equation







































Also known as Radiative Transport Equation













Also known as Radiative Transport Equation













































Single scattering: compute $T_r(x_L, x_t)$ to light source



Conventional Rendering







Exponential Fog







Single Scattering











Multiple scattering: compute random walk





Sample phase function $p(x, \vec{\omega}, \vec{\omega}')$

e.g. Henyey-Greenstein
$$p(\theta) = \frac{1}{4\pi} \frac{1-g^2}{(1+g^2-2g\cos\theta)^{3/2}}$$

by inversion $\cos\theta = \frac{1}{2g} \left(1+g^2-\left(\frac{1-g^2}{1-g+2g\xi}\right)^2\right)$

- For a given direction, choose a distance d to travel based on $T_r(\,,\,,\,)$
 - If d is closer than the nearest surface \rightarrow scatter
 - If not, compute surface radiance





Distance d is given by the free-flight distance Sample with $d = \frac{-\ln(1-\xi)}{\sigma_t}$ (homogeneous media)





color **VPT**(o, ω) $s = nearestSurfaceDist(o, \omega)$ d = $-ln(1 - random()) / \sigma_+$ if (d<s) // Media scattering $o += d^*\omega$ return $\sigma_s / \sigma_t * VPT(o, samplePhase())$ else // Surface scattering

o += s*W $(\omega_i, pdf_i) = sampleBRDF(o, \omega)$ return BRDF(o, ω_i) * VPT(o, ω_i) / pdf_i







Questions?



